

# Spin tracking vs Integration and dependence on $\beta$ -amplitude

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## E field correction

3 ways to compute *E*-field contribution to  $\omega_a$

1. Spin tracking (BMT equation)

2. Integration 
$$\vec{C}_e(T) \sim 2 \frac{\Delta p}{p} \frac{1}{T} \int_0^T \frac{\vec{\beta} \times \vec{E}}{Bc} dt$$

a) Integration along trajectory (includes betatron oscillations)

b) Integration along closed orbit ( $x = \eta\delta$ )

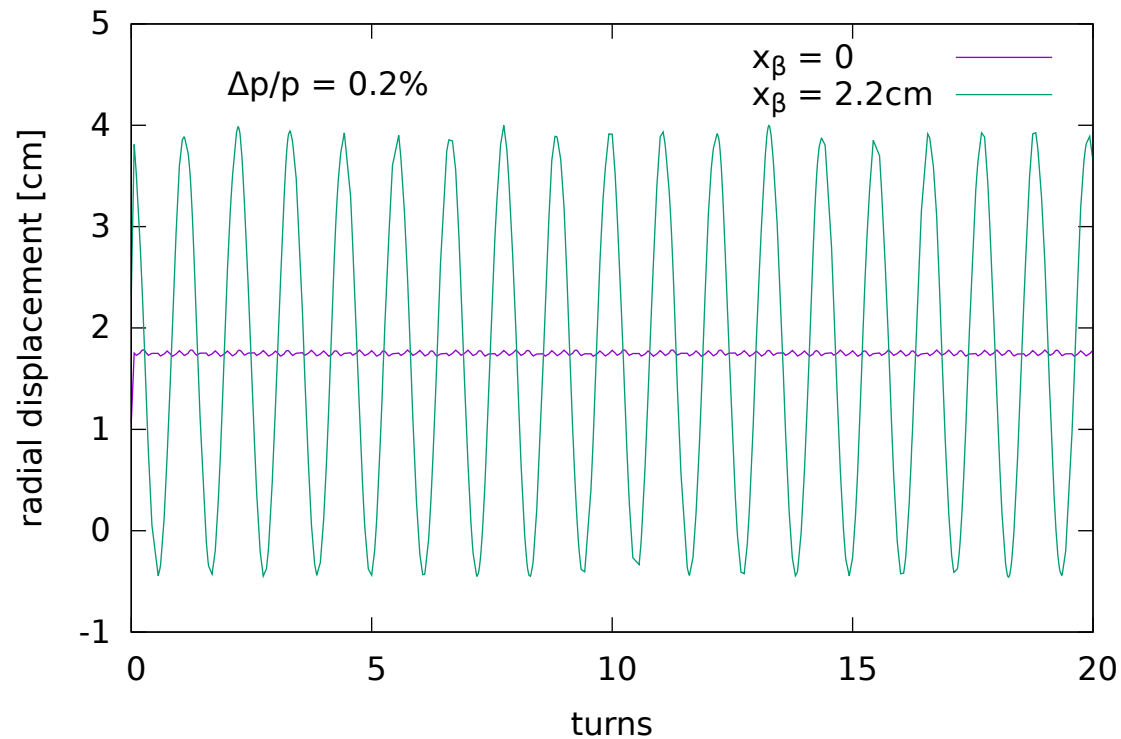
Note that method 2b) is most nearly equivalent to the ‘classic’ method, namely

$$C_E = -2\beta^2 n(1-n) \frac{\langle x_e^2 \rangle}{r_0^2}$$

Compare the 3 methods in simulation to determine

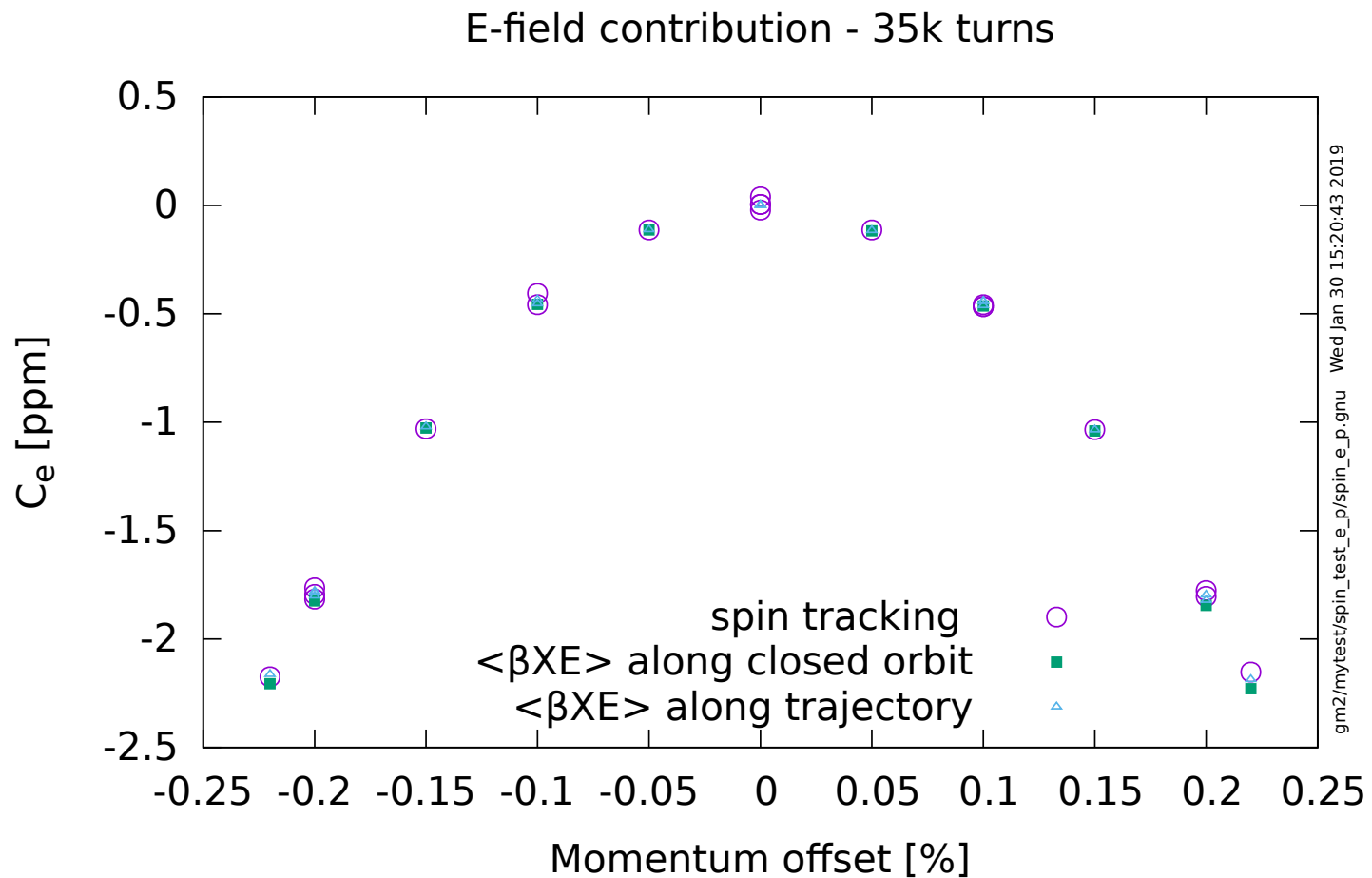
1. If integration is a reliable proxy for spin tracking

2. The size of the contribution from finite betatron oscillation amplitude



Distinct trajectories with common momentum offset

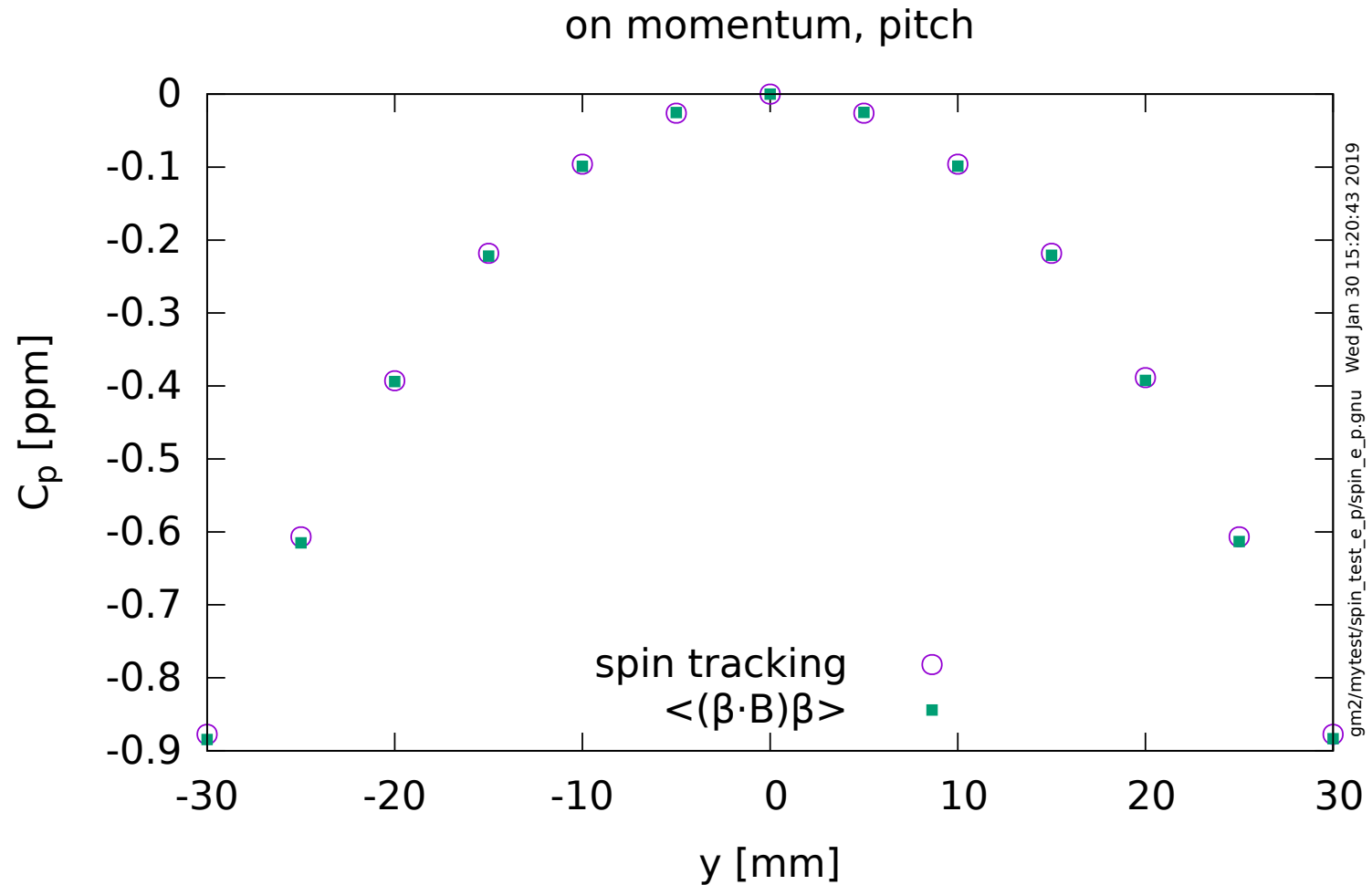
- For trajectory compute  $\omega_a$  by spin tracking and by integration



Multiple trajectories at each momentum with minimum and maximum betatron amplitude

Conclusion

- Integration is equivalent to spin tracking
- Amplitude dependence is  $< 50$  ppb



### Conclusion

- Spin tracking is equivalent to integration

Next - compare spin tracking and integration

- With Misaligned quads
- Vs Quad voltage
- During/after scraping